

## 6.4 Rational Equations Filled In.notebook

December 01, 2017

Quiz 6.3

(6 points) Simplify the complex rational expression using ~~both~~ Method I and Method II. State which method you prefer for the problem.

$$\frac{1 - \frac{a}{a-2}}{2 - \frac{a+2}{a}}$$

$$43) \quad \frac{x+1}{x^2 - 6xy + 9y^2} + \frac{x+2y}{x^2 - 2xy - 3y^2}$$

LCD:  $(x-3y)(x+3y)(x+y)$

$$\frac{(x+y)(x+3y)}{(x-3y)(x+3y)(x+y)} + \frac{(x+2y)(x-3y)}{(x-3y)(x+3y)(x+y)(x-3y)}$$

$$\frac{x^2 + 2xy + y^2 + x^2 - xy - 6y^2}{(x-3y)^2(x+y)} =$$

LCD

$\begin{array}{r} -10 \\ -1 \\ 1 \\ 2 \\ -2 \end{array} \left| \begin{array}{r} 10 \\ 10 \\ 5 \\ 5 \end{array} \right. \quad \begin{array}{r} 10 \\ 10 \\ 5 \\ 5 \end{array}$

$x(x-1)^2$

$$53) \quad \frac{2(x-1)^2}{x(x-1)^2} - \frac{2x(x-1)}{x(x-1)^2} + \frac{3x}{x(x-1)^2}$$

$$2(x^2 - 2x + 1) - 2x^2 - 2 = 3x$$

Feb 1-7:06 AM

Nov 30-1:01 PM

$LCD: (x-3)(x-2)$  6.4 Rational Equations

Solve (make sure to check for extraneous answers)

$$\frac{2x-1}{x-3} = \frac{2(x+1)}{x-2}$$

$$\frac{(2x-1)(x-2)}{(x-3)(x-2)} = \frac{2(x+1)(x-3)}{(x-3)(x-2)} \quad \cancel{(x-3)(x-2)}$$

$$\cancel{(2x-1)(x-2)} = 2(x+1)(x-3)$$

$$2x^2 - 5x + 2 = 2(x^2 - 2x - 3)$$

$$\cancel{\frac{2x^2 - 5x + 2}{2x^2 + 5x + 6}} = \cancel{\frac{2x^2 - 4x - 6}{2x^2 + 5x + 6}}$$

$8 = x$

You try

$$\frac{x-4}{x^2+4} = \frac{3}{3x+2} \quad x \neq -\frac{2}{3}, 2i, -2i$$

$$(x-4)(3x+2) = 3(x^2+4)$$

$$\frac{3x^2 - 10x - 8}{-3x^2 + 8} = \frac{3x^2 + 12}{-3x^2 + 8}$$

$-10x = 20$

$$x = -2$$

Feb 1-7:08 AM

Feb 1-7:18 AM

Note: There is a big difference between a rational expression and equation. They are not computed the same. Watch out for this on the test!

Solve: LCD:  $6x$

$$\frac{2}{x} - \frac{1}{6} = \frac{5}{2x} - \frac{1}{3}$$

$$2(6) - 1(6x) = 5(3) - 1(2x)$$

$$\begin{array}{r} 12 - x = 15 - 2x \\ -12 + 2x \quad -12 + 2x \\ \hline x = 3 \end{array}$$

Feb 1-7:12 AM

Feb 1-7:16 AM

You try

$$\frac{5}{x} + \frac{1}{4} = \frac{3}{2x} - \frac{3}{2}$$

Solve LCD:  $(p-3)(p-1)(p+1)$

$$\frac{3}{p^2 - 4p + 3} + \frac{6}{p^2 - 2p - 3} = \frac{5}{p^2 - 1}$$

$$\frac{3}{(p-3)(p-1)} + \frac{6}{(p-3)(p+1)} = \frac{5}{(p+1)(p-1)}$$

$$3(p+1) + 6(p-1) = 5(p-3)$$

$$3p+3 + 6p-6 = 5p-15$$

$$\begin{array}{r} 9p - 3 = 5p - 15 \\ -5p + 3 - 5p + 3 \\ \hline 4p = -12 \end{array}$$

$$(p = -3)$$

Feb 1-7:20 AM

Feb 1-7:21 AM

You try

$$\frac{3}{x^2 + 5x + 4} + \frac{2}{x^2 - 3x - 4} = \frac{4}{x^2 - 16}$$

Solve:

$$\frac{w+3}{w-1} + \frac{w+5}{w} = \frac{3w+1}{w-1}$$

Feb 1-7:22 AM

Feb 1-7:23 AM

You Try

$$\frac{z+1}{z+4} + \frac{z+1}{z-3} = \frac{z^2 + z + 16}{z^2 + z - 12}$$

For the function  $f(x) = x + \frac{4}{x}$ , solve  $f(x) = 5$ . What point(s) are on the graph of  $f$ ?

$$\frac{5x}{x} = \frac{x^2}{x} + \frac{4}{x}$$

$$5x = x^2 + 4$$

$$x^2 - 5x + 4 = 0$$

$$(x-4)(x-1) = 0$$

$$x = 4, 1$$

$$(4, 5) \quad (1, 5)$$

Feb 1-7:31 AM

Feb 1-7:39 AM

The concentration  $C$  of a drug in a patient's bloodstream in milligrams per liter  $t$  hours after ingestion is modeled by

$$C(t) = \frac{40}{t^2 + 9}$$

When will the concentration of the drug be 4 milligrams per liter?

$$(2^2+9)4 = \frac{40}{t^2+9}$$

$$4t^2 + 36 = 40$$

$$4t^2 - 4 = 0$$

$$4(t^2 - 1) = 0$$

$$4(t-1)(t+1) = 0$$

$$t = 1, \cancel{t = -1}$$

After 1 hour, the concentration is 4 mg

You try

For the function  $f(x) = 2x - \frac{3}{x}$ , solve  $f(x) = 1$ . What point(s) are on the graph of  $f$ ?

Feb 1-10:00 AM

Feb 1-10:02 AM

Nov 30-1:34 PM