

## 4-2 Finite Geometric Series

Objectives:

- I can write a series using sigma notation
- I can find the sum of a series

Warm - up

1. Write a recursive rule and an explicit rule for the sequence:

9, 27, 81, 243

$$f(n) = 9(3)^{n-1}$$

2. Find the stated term of the geometric sequence:

-3, -6, -12, -24, ... ; 9<sup>th</sup> term

$$f(n) = -3(2)^{n-1}$$

$$f(9) = -3(2)^{9-1}$$

$$= -3(2)^8$$

$$= -768$$

Jun 3-1:09 PM

Jan 4-4:52 PM

You have 2 biological parents, 4 biological grandparents, and 8 biological great-grandparents. How many great-great-great-great grandparents (6<sup>th</sup> generation) do you have?

2, 4, 8, 16, 32, 64

$$f(n) = 2(2)^{n-1}$$

How many total ancestors do you have if you trace your ancestry back 6 generations?

$$2 + 4 + 8 + 16 + 32 + 64 = 126$$

Jun 3-1:20 PM

Series: adding together all the numbers in a sequence

Last Term Number

$$\sum_{k=1}^n a_k$$

First Term Number

Explicit Rule

Summation notation:  $\sum_{k=1}^n a_k = a_1 + a_2 + a_3 + \dots + a_n$

Dec 15-8:53 AM

Find the following sums:

$$\begin{aligned} \text{a. } \sum_{k=1}^5 3k &= 3(1) + 3(2) + 3(3) + 3(4) + 3(5) \\ &= 3 + 6 + 9 + 12 + 15 \\ &= 45 \end{aligned}$$

$$\text{b. } \sum_{k=5}^8 k^2$$

$$\text{c. } \sum_{k=3}^7 4k + 1$$

### Process

- Determine the common ratio
- Write an explicit rule
- Figure out how many total terms
- Write in sigma notation
- Evaluate on calculator

\*Under math button on the calculator\*

Jun 3-1:34 PM

Aug 23-3:21 PM

Write the following in sigma notation and then find the sum  $\sum$

A geometric series that begins with 3, a common factor of 2, with 6 terms

$$\sum_{n=1}^6 (3(2)^{n-1}) =$$

A geometric series that begins with 5, a common factor of 3, with 7 terms

$$\sum_{n=1}^7 (5(3)^{n-1})$$

Find the sum of the series:

$$\begin{array}{ccccccc} 1 & 2 & 3 & & 6 & & 4 & 5 \\ 4, & 8, & 16, & \dots, & 128 & & 32, & 64 \end{array}$$

$$\sum_{n=1}^6 (4(2)^{n-1}) = 252$$

$$\begin{array}{ccccccc} 1 & 2 & 3 & & 6 & & 4 & 5 \\ 3, & 9, & 27, & \dots, & 729 & & 81, & 243 \end{array}$$

Jan 7-10:51 AM

Jun 3-1:36 PM

Find the sum of the series

2, -8, 32, ..., -2048

-3, 6, -12, ..., 96

Aug 23-3:26 PM