

Welcome! Choose your seat to be you assigned seat for the next while.

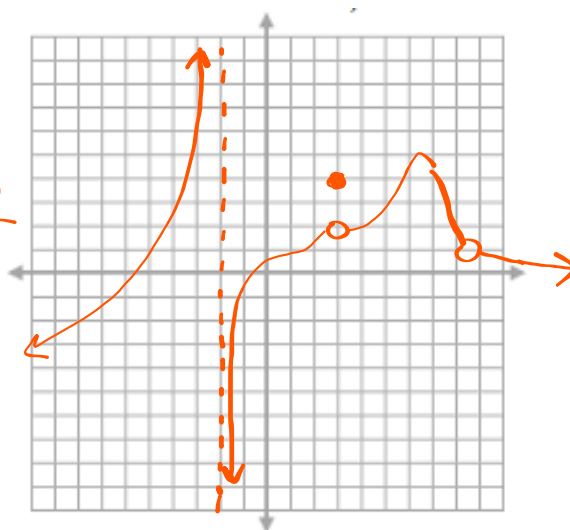
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Work on this by yourself or with a partner.

Does the limit exist at $x = 3$? Explain why or why not.

$$\lim_{x \rightarrow 3} f(x) = 2$$

$$f(3) = 4$$



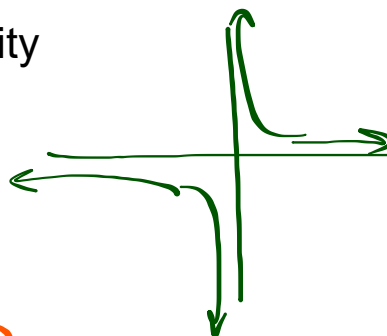
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2.2 Limits to Infinity

Use the table on your calculator to investigate the limit numerically:

$$\lim_{x \rightarrow \infty} \frac{1}{x} = 0$$

$$\lim_{x \rightarrow -\infty} \frac{1}{x} = 0$$



Definition of a Horizontal Asymptote:

$$\lim_{x \rightarrow \infty} f(x) = b$$

If *or*

then there is a HA at $y = b$

$$\lim_{x \rightarrow -\infty} f(x) = b$$

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Estimate: (remember this includes both the left and right hand limits!)

$$\lim_{x \rightarrow 0^+} \frac{1}{x} = \infty$$

$$\lim_{x \rightarrow 0^-} \frac{1}{x} = -\infty$$

$$\lim_{x \rightarrow 0} \frac{1}{x} = \text{DNE}$$

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Definition of a Vertical Asymptote:

$$\lim_{x \rightarrow a^+} f(x) = \pm\infty$$

or

$$\lim_{x \rightarrow a^-} f(x) = \pm\infty$$

then there is a VA at $x = a$

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Summary of finding asymptotes

Horizontal Asymptotes:

1. If degree of the numerator is < the degree of the denominator: $y=0$ $\frac{x}{x^2}$
 "bottom heavy" $y=0$

2. If degree of the numerator is = to the degree of the denominator: $y=$

divide leading coefficients $\frac{2x}{x} \quad y=2$

3. If degree of the numerator is > the degree of the denominator: $y=\text{quotient}$

$$\frac{x^2-1}{x+1} = \frac{(x+1)(x-1)}{x+1} = \textcircled{x-1} \text{ EBM}$$

Vertical Asymptotes:

Domain restrictions can't div by 0, no negs in $\sqrt{\quad}$

set denom = 0

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Power Function End Behavior Models:

$f(x) = \frac{x^2 - 1}{x + 2}$

VA: $x = -2$ PF: $y = x$

Graph $f(x)$ using the following windows:

Synthetic Division

-2	1	0	-1
		-2	4
	1	-2	3

EBM: $(x - 2) + \frac{3}{x + 2}$

what is an end-behavior model for $f(x)$:

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Find all asymptotes and describe them using limits. Find a power function that resembles $f(x)$.

1. $f(x) = \frac{x+4}{x^2-9} = \frac{x+4}{(x-3)(x+3)}$

VA: $x = 3, x = -3$

HA: $y = 0$

$\lim_{x \rightarrow 3^+} f(x) = \infty$

$\lim_{x \rightarrow -3^+} f(x) = -\infty$

2. $f(x) = \frac{2x^2 + 3x - 1}{x^2 - 4}$

3. $f(x) = \cos\left(\frac{1}{x}\right)$

HA: $y = 1$

PF: None

$\lim_{x \rightarrow \infty} f(x) = 1$

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$$4. f(x) = \frac{2x-1}{|x|-3} = 0$$

$$VA: x = 3, -3$$

$$HA: y = 2, -2$$

$$PF: \frac{2x}{x} \quad y = 2$$

$$6. f(x) = \frac{4x^3 + 2x - 1}{x + 3}$$

$$5. f(x) = \frac{5x + \sin x}{x}$$

$$f(x) = \frac{5x}{x} + \frac{\sin x}{x}$$

$$HA: \frac{5}{1} \leq 0 \quad y = 5$$

$$VA: x = 0$$

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