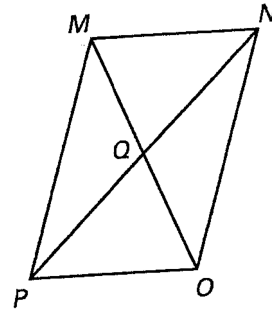
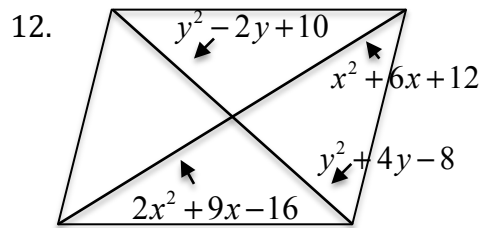
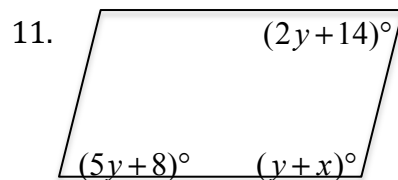
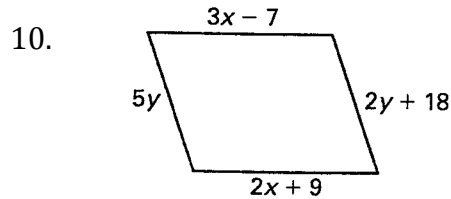
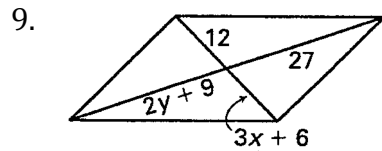


Use the diagram of parallelogram $MNOP$ at the right. Complete the statement and give a reason.

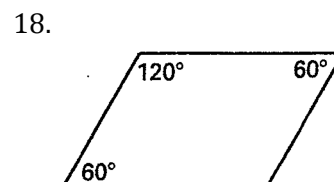
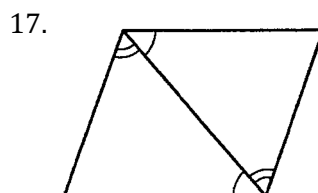
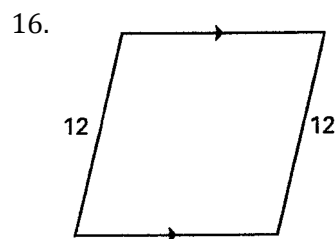
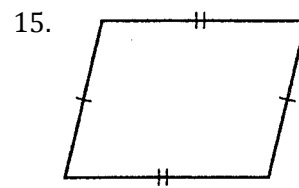
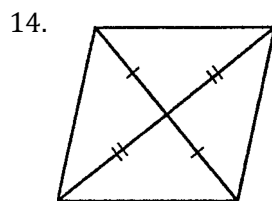
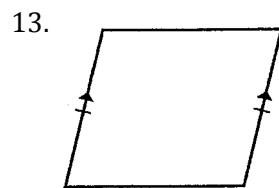


1. $\overline{MN} \cong$ Reason:
2. $MN \parallel$ Reason:
3. $\overline{ON} \cong$ Reason:
4. $\angle MPO \cong$ Reason:
5. $\overline{PQ} \cong$ Reason:
6. $\overline{QM} \cong$ Reason:
7. $\angle MQN \cong$ Reason:
8. $\angle NPO \cong$ Reason:

Find the value of each variable in the parallelogram.



Are you given enough information to determine whether the quadrilateral is a parallelogram?

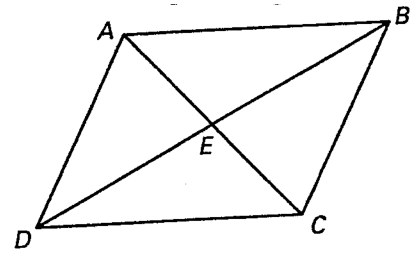


19. Prove that if a quadrilateral is a parallelogram then the opposite angles are congruent. You may use a flow or two-column proof to do this.

Hint: You can use $\triangle ADC$ and $\triangle ABC$ and the fact that you know that opposite sides of a parallelogram are congruent to prove this. Or you can use parallel transversals to prove this.

Given: Parallelogram ABCD with diagonals that meet at E

Prove: $\angle ADC \cong \angle ABC$

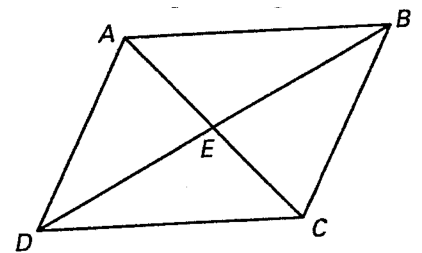


20. Prove that if you know that the opposite sides of a quadrilateral are congruent then it is a parallelogram.

Hint: use congruent triangles and the Alternate angle converse theorem twice.

Given: $\overline{DA} \cong \overline{CB}$ and $\overline{AB} \cong \overline{DC}$

Prove: $\overline{DA} \parallel \overline{CB}$ and $\overline{AB} \parallel \overline{DC}$



Answer Key (Not all odds):

1. $\overline{MN} \cong \overline{OP}$, Reason: In a parallelogram opposite sides are \cong
5. $\overline{PQ} \cong \overline{NQ}$, Reason: In a parallelogram diagonals bisect each other
7. $\angle MQN \cong \angle OQP$ Vertical \angle 's
9. $y = 9, x = 2$
11. $x = 160, y = 2$
13. yes
17. yes