

## 6-1: Properties of Logarithms

6-1a: I can use the properties of exponents to simplify and evaluate logarithms.

6-1b: I can use the properties of logarithms to simplify and evaluate logarithms.

**EXPONENT RULES***Graphic Organizer*

Name	Rule	Examples
<b>ADDING &amp; SUBTRACTING MONOMIALS</b>	<b>COMBINE LIKE TERMS!!!</b> (DO NOT CHANGE common variables and exponents!)	1. $9x^2y - 10x^2y =$ 2. Subtract $6w$ from $8w$ .
<b>PRODUCT RULE</b>	$x^a \cdot x^b =$	1. $h^2 \cdot h^6 =$ 2. $(-2a^2b) \cdot (7a^3b) =$
<b>POWER RULE</b>	$(x^a)^b =$	1. $(x^2)^3 =$ 2. $(-2m^5)^2 \cdot m^3 =$
<b>QUOTIENT RULE</b>	$\frac{x^a}{x^b} =$	1. $\frac{27x^5}{42x} =$ 2. $\frac{(y^2)^2}{y^4} =$
<b>NEGATIVE EXPONENT RULE</b>	$x^{-a} =$	1. $-5x^{-2} =$ 2. $\frac{4k^2}{8k^5} =$
<b>ZERO EXPONENT RULE</b>	$x^0 =$	1. $7x^0 =$ 2. $\frac{(w^4)^2}{w^8} =$

## 5-2 Rules of Logarithms

Name	Property	Examples
Zero Rule	$\log_a 1 =$	$\log_5 1 =$ $\ln 1 =$
Identity Rule	$\log_a a =$	$\log_4 4 =$ $\log 10 =$
Inverse Properties	$\log_a a^r =$ $b^{\log_b M} =$	$\log_4 4^3 =$ $\ln e^{-0.5} =$ $5^{\log_5 20} =$ $e^{\ln 24} =$
Product Rule	$\log_b MN =$	$\log_2 5 * 3 =$ $\log 5w =$ $\ln 6z =$
Quotient Rule	$\log_b \frac{M}{N} =$	$\log_7 \frac{9}{x} =$ $\ln \frac{p}{3} =$
Power Rule	$\log_b M^r =$	$\log_8 3^5 =$ $\log_b 5 =$

Find the value of each logarithm without using a calculator.

1.  $\log_7 7$

2.  $\log_{18} 18$

3.  $\log_5 1$

4.  $\log_9 1$

$$\log_a 1 = 0 \quad \log_a a = 1$$


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$$\log_5 1$$

$$\ln 1$$

$$\log_4 4$$

$$\log 10$$

- $\log_3 3^2$

- $\log_5 5^8$

Without evaluating, predict what the following logs equal:

- $\log_2 2^{10}$

- $\log_{20} 20^7$

$$\log_a a^r = r$$

$$\log_4 4^3$$

$$\ln e^{-0.5}$$

Recall:  $b^x = a \iff \log_b a = x$

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$$5^{\log_5 20}$$



$$b^{\log_b M} = M \quad b \neq 0$$

$$5^{\log_5 20}$$

$$8^{\log_8 \sqrt{23}}$$

$$12^{\log_{12} \sqrt{2}}$$

$$10^{\log 0.2}$$

$$\log_b(MN) = \log_b M + \log_b N$$

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$$\log_2(5 \cdot 3)$$

$$\ln(6z)$$

Find 3 ways to expand  $\log_3 24$   
using this rule



$$\log_b \frac{M}{N} =$$

$$\log_b \left( \frac{M}{N} \right) = \log_b M - \log_b N$$

$$\log_2 \left( \frac{5}{3} \right)$$

$$\log \left( \frac{y}{5} \right)$$

Find 3 ways to expand  $\log_5 3$   
using this rule

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$$\log_3\left(\frac{4x}{y}\right)$$

$$\log_3\left(\frac{3m}{n}\right)$$

$$\log_3\left(\frac{q}{3p}\right)$$

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$$\log_2(4)^3 = 3 \cdot \log_2 4$$

$$M \quad b \quad b \neq 0$$

$$\log_b M^r = r \log_b M$$

$$\log_8 3^5$$

$$\ln x^{\sqrt{3}}$$

$$\log_5 25$$

$$\log b^5$$



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$$\log_2(x^2y^3)$$

$$\log_6 \frac{x^2}{y^3}$$

$$\log_a 1 = 0 \quad \log_a a = 1$$

$$M \quad b \quad b \neq 0$$

$$\log_b M^r = r \log_b M$$

$$b \quad r \quad b \neq 0$$

$$\log_a a^r = r$$

$$MN \quad b \quad b \neq 0$$

$$\log_b \left( \frac{M}{N} \right) = \log_b M - \log_b N$$

$$b \quad M \quad b \neq 0$$

$$\log_{20} 20^7$$

$$b^{\log_b M} = M$$

$$N \quad b \quad b \neq 0$$

$$\log_b (MN) = \log_b M + \log_b N$$

Day 2

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$$\log_5 \left( a^{-2} b c^3 \right)^{-2}$$

$$\log \left( a^2 \sqrt{bc} \right)$$

$$\log \left( \frac{100x}{\sqrt{y}} \right)$$

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$$\log_6 3 + \log_6 12$$

$$\log(x - 2) - \log x$$

$$\log_5 x - 3\log_5 2$$

$$\log(x - 1) + \log(x + 1) - 3\log x$$

