

5-3 Solving Exponential and Logarithmic equations

Objectives:

5-3a: I can solve exponential and logarithmic equations graphically.

5-3b: I can solve exponential and logarithmic equations algebraically.

Jan 3-2:07 PM

RECALL: Solving Graphically

$$275e^{0.06x} = 1000$$

$$y_1 = \quad \quad y_2 =$$

$$10^{2x} = 1500$$

$$y_1 = \quad \quad y_2 =$$

Jan 3-2:08 PM

Now you try...solve the exponential & logarithmic equations graphically.

$$20^{2r} = 56$$

$$y_1 = \quad y_2 =$$

$$e^{.23x} = 1.99$$

$$y_1 = \quad y_2 =$$

Inverses

Addition/Subtraction	Natural Log/e [^]	Common Log/10 [^]	Log base b/b [^]
$x - 5 = 10$	$e^x = 5$	$10^x = 100$	$2^x = 16$
$x + 7 = 21$	$\ln x = 7$	$\log x = 3$	$\log_3 x = 4$

Solve the following equations

$$10 = 5e^{4x}$$

$$5^{x-1} - 4 = 7$$

$$\log_3(2x - 4) = 4$$

$$6^{3x} = 12$$

Jan 3-2:58 PM

Solve the following

$$\ln(x + 12) = 3 \ln 2$$

$$\log(4x) = 2$$

$$4 \ln(x + 7) - 5 = 1$$

Jan 3-3:04 PM

Solve the following

$$\log(x + 2) - 3 = 5$$

$$\log_4(x - 1) = 1$$

Jan 3-3:11 PM

Compound Interest Formula

$$A(t) = P \left(1 + \frac{r}{n} \right)^{nt}$$

P is the principal

r is the annual interest rate

n is the number of compounding periods per year

t is the time in years

Feb 15-11:03 AM

Many banks compound the interest on accounts daily or monthly. However, some banks compound interest continuously, or at every instant, by using the *continuous compounding formula*.

Continuous Compounding Formula

If P dollars are invested at an interest rate r , that is compounded continuously, then the amount, A , of the investment at time t is given by

$$A(t) = Pe^{rt}$$

P is principal (initial value)

r is interest rate

t is time (in years)

Feb 15-11:03 AM

How long will it take for a \$250 initial investment in an account that pays 4.5% compounded continuously to grow to \$750?

Suppose that \$250 is deposited into an account that pays 4.5% compounded quarterly. Solve for t to find how long it will take for the account to contain at least \$500.

Jan 3-3:03 PM

Comparing acidity: $pH = -\log[H^+]$

$[H^+]$ = hydrogen-ion concentration

Vinegar has a pH of 2.4. What is its hydrogen ion concentration?

Baking soda has a pH of 8.4. What is its hydrogen ion concentration?

Which has a higher hydrogen ion concentration?

Feb 3-11:00 AM

Nov 12-1:49 PM