

## 1-5 Adding, Subtracting, and Multiplying Radical expressions

## Product Property of Radicals

If  $\sqrt[n]{a}$  and  $\sqrt[n]{b}$  are real numbers, and  $n \geq 2$  is an integer, then

$$\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{ab}$$

$$\sqrt[3]{8} \cdot \sqrt[3]{27} = \sqrt[3]{18}$$

We can prove this using rational exponents.

Note:  $\sqrt{a+b} \neq \sqrt{a} + \sqrt{b}$

Feb 23-6:34 AM

Simplify

$$\sqrt{5} \cdot \sqrt{3} = \sqrt{15}$$

$$\sqrt[3]{2} \cdot \sqrt[3]{13} = \sqrt[3]{26}$$

$$\sqrt{3} + \sqrt{5}$$

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Multiply

$$\sqrt[5]{6c} \cdot \sqrt[5]{7c^2} = \sqrt[5]{42c^3}$$

$$c^1 \cdot c^2 = c^3$$

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You try

$$\sqrt{11} \cdot \sqrt{7}$$

$$= \sqrt{77}$$

$$\sqrt[4]{6} \cdot \sqrt[4]{7}$$

$$= \sqrt[4]{42}$$

$$\sqrt[7]{5p^1} \cdot \sqrt[7]{4p^3}$$

$$\sqrt[7]{20p^4}$$

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Multiply and Simplify Assuming all variables are greater than or equal to zero.

$$\sqrt{3} \cdot \sqrt{15}$$

$$= \sqrt{45} \quad \boxed{3\sqrt{5}}$$

$$\sqrt[3]{4x} \cdot \sqrt[3]{2x^4}$$

$$2 \cdot 3 \sqrt[3]{8x^5} \quad \boxed{6x\sqrt{x^2}}$$

$$\sqrt[4]{27a^2b^5} \cdot \sqrt[4]{6a^3b^6}$$

$$\sqrt[4]{162a^5b^{11}}$$

Handwritten prime factorization for  $\sqrt[4]{162a^5b^{11}}$ :

- 162 is factored into  $2 \cdot 3^4$ .
- $a^5$  is factored into  $a^4 \cdot a$ .
- $b^{11}$  is factored into  $b^8 \cdot b^3$ .

$$\boxed{3ab^2\sqrt[4]{2ab^3}}$$

$$aaaa$$

Feb 23-7:10 AM

You try

$$\sqrt{6} \cdot \sqrt{8} = \sqrt{48}$$

$$\boxed{4\sqrt{3}}$$

Handwritten prime factorization for  $\sqrt{48}$ :

- 48 is factored into  $2^4 \cdot 3$ .

$$4\sqrt[3]{8a^2b^5} \cdot \sqrt[3]{6a^2b^4}$$

$$4\sqrt[3]{48a^4b^9}$$

Handwritten prime factorization for  $4\sqrt[3]{48a^4b^9}$ :

- 48 is factored into  $2^4 \cdot 3$ .
- $a^4$  is factored into  $a^3 \cdot a$ .
- $b^9$  is factored into  $b^6 \cdot b^3$ .

$$4 \cdot 2ab^3\sqrt[3]{6a} = \boxed{8ab^3\sqrt[3]{6a}}$$

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## Quotient Property of Radicals

If  $\sqrt[n]{a}$  and  $\sqrt[n]{b}$  are real numbers,  $b \neq 0$ ,  $n \geq 2$  is an integer, then

$$\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$$

We can prove this using rational exponents.

Feb 23-7:14 AM

Simplify Assuming all variables are greater than or equal to zero.

$$\sqrt{\frac{18}{25}}$$

$$\sqrt[3]{\frac{6z^3}{125}}$$

$$\sqrt[4]{\frac{10a^2}{81b^4}}$$

Feb 23-7:20 AM

You try

$$\sqrt{\frac{13}{49}}$$

$$\sqrt[3]{\frac{27p^3}{8}}$$

$$\sqrt[4]{\frac{3q^4}{16}}$$

Feb 23-8:24 AM

Simplify Assuming all variables are greater than or equal to zero.

$$\frac{\sqrt{24a^3}}{\sqrt{6a}}$$

$$\frac{-2\sqrt[3]{54a}}{\sqrt[3]{2a^4}}$$

$$\frac{\sqrt[3]{-375x^2y}}{\sqrt[3]{3x^{-1}y^7}}$$

Feb 23-8:25 AM

You try

$$\frac{\sqrt{12a^5}}{\sqrt{3a}}$$

$$\frac{\sqrt[3]{-24x^2}}{\sqrt[3]{3x^{-1}}}$$

$$\frac{\sqrt[3]{250a^5b^{-2}}}{\sqrt[3]{2ab}}$$

Feb 23-8:27 AM

## 7.5 Rationalizing Radical Expressions

Rationalize the denominator of each expression:

Assume all variables are positive.

$$\frac{1}{\sqrt{7}}$$

$$\frac{\sqrt{5}}{\sqrt{12}}$$

$$\frac{2}{3\sqrt{2x}}$$

Mar 2-9:50 AM

You Try

$$\frac{1}{\sqrt{3}}$$

$$\frac{\sqrt{5}}{\sqrt{8}}$$

$$\frac{5}{\sqrt{10x}}$$

Mar 2-9:56 AM

Add the following

$$5\sqrt{2x} + 9\sqrt{2x}$$

$$3\sqrt[3]{10} + 7\sqrt[3]{10} - 5\sqrt[3]{10}$$

Feb 24-9:59 AM

You Try

$$9\sqrt{13y} + 4\sqrt{13y}$$

$$4\sqrt[4]{5} + 9\sqrt[4]{5} - 3\sqrt[4]{5}$$

Feb 24-10:03 AM

Add or subtract as indicated. Assume all variables are real numbers greater than or equal to zero

$$3\sqrt{12} + 7\sqrt{3}$$

Feb 24-10:04 AM

Add or subtract as indicated. Assume all variables are real numbers greater than or equal to zero

$$3x\sqrt{20x} - 7\sqrt{5x^3}$$

$$3\sqrt{5} + 7\sqrt{13}$$

Feb 24-10:05 AM

You try

$$7\sqrt{10} - 6\sqrt{3}$$

$$4\sqrt{14} - 3\sqrt{8}$$

$$-5x\sqrt[3]{54x} + 7\sqrt[3]{2x^4}$$

Feb 24-10:06 AM

Add or subtract as indicated. Assume all variables are real numbers greater than or equal to zero

$$\sqrt[3]{16x^4} - 7x\sqrt[3]{-2x} + \sqrt[3]{54x}$$

Feb 24-10:06 AM

You try

$$\sqrt[3]{8z^4} - 2z\sqrt[3]{-27z} + \sqrt[3]{125z}$$

Feb 24-10:10 AM

Multiply and simplify

$$\sqrt{5}(3 - 4\sqrt{5})$$

$$\sqrt[3]{2}(3 + \sqrt[3]{4})$$

Feb 24-10:17 AM

You try

$$\sqrt{6}(3 - 5\sqrt{6})$$

$$\sqrt[3]{12}(3 - \sqrt[3]{2})$$

Feb 24-10:20 AM