

1-4 Rational Exponents

Rational exponent Calc task

$$1^{\frac{1}{2}} = 1 \quad 4, 9, 16, 25, 36$$

$$4^{\frac{1}{2}} = 2 \quad a^{\left(\frac{1}{2}\right)} = \sqrt{a}$$

$$9^{\frac{1}{2}} = 3$$

$$16^{\frac{1}{2}} = 4$$

:

1, 8, 27, 64, 125, 216

$$\begin{aligned} 1^{\frac{1}{3}} &= 1 \\ 8^{\frac{1}{3}} &= 2 \\ 27^{\frac{1}{3}} &= 3 \\ 64^{\frac{1}{3}} &= 4 \\ &\vdots \end{aligned}$$

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1, 8, 27, 64, 125, 216

$$a^{\left(\frac{2}{3}\right)} = \sqrt[3]{a^2}$$

power
root

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1, 16, 81, 256, 625, 1296

$$a^{\left(\frac{3}{4}\right)} = \sqrt[4]{a^3}$$

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$$a^{\left(\frac{m}{n}\right)} = \sqrt[n]{a^m}$$

Fractional exponent

$$a^{\frac{1}{n}} = \sqrt[n]{a}$$

n is an integer bigger than or equal to 2

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Feb 15-8:55 AM

Write each of the following as a radical and simplify, if possible.

$$9^{\frac{1}{2}} = \sqrt{9} = 3 \quad (-64)^{\frac{1}{3}}$$

$$\sqrt[3]{-64} = -4$$

$$100^{\frac{1}{2}} \quad -100^{\frac{1}{2}} \quad z^{\frac{1}{2}}$$

$$\sqrt[4]{100^2} = \sqrt{100}$$

$$= 10$$

Feb 15-9:05 AM

You try

$$25^{\frac{1}{2}} \quad (-27)^{\frac{1}{3}}$$

$$-64^{\frac{1}{2}} \quad b^{\frac{1}{2}}$$

Feb 15-9:08 AM

Rewrite in exponent form

$$\sqrt[7]{x^4} = x^{\frac{4}{7}}$$

$$\sqrt[4]{b} = b^{\frac{1}{4}}$$

Feb 15-9:10 AM

You try

$$\sqrt[12]{r} \quad \sqrt[5]{d}$$

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$$a^{\frac{m}{n}} = \sqrt[n]{a^m} = \left(\sqrt[n]{a}\right)^m$$

a is real, m/n is a rational number in lowest terms with n bigger or equal to 2

Write each of the following as a radical and simplify, if possible.

$$25^{\frac{3}{2}} \quad 64^{\frac{2}{3}} \quad -9^{\frac{5}{2}}$$

$$\sqrt[3]{25^3} = 25 \quad \sqrt[3]{64^2} = 64^{\frac{2}{3}}$$

$$(-8)^{\frac{7}{3}} = -81^{\frac{1}{2}}$$

$$5^3 = 125$$

$$2^4 = 16$$

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Feb 15-9:35 AM

You try

$$27^{\frac{2}{3}}$$

$$16^{\frac{3}{2}}$$

$$-25^{\frac{5}{2}}$$

$$-16^{\frac{3}{4}}$$

Rewrite in exponent form

$$\sqrt[3]{x^2} = x^{\frac{2}{3}} \quad \left(\sqrt[4]{r}\right)^2 = r^{\frac{2}{4}} = r^{\frac{1}{2}}$$

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You try

$$\sqrt[8]{a^3}$$

$$\left(\sqrt[3]{h}\right)^9$$

$$a^{-\frac{m}{n}} = \frac{1}{a^{\frac{m}{n}}} \quad \text{and} \quad \frac{1}{a^{-\frac{m}{n}}} = a^{\frac{m}{n}}$$

$\frac{m}{n}$ is a rational number, and a is a nonzero real number

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Write each of the following as a radical and simplify, if possible.

$$x^{-\frac{1}{3}} = \frac{1}{x^{\frac{1}{3}}} = \frac{1}{\sqrt[3]{x}}$$

$$36^{-\frac{1}{2}} = \frac{1}{36^{\frac{1}{2}}} = \frac{1}{\sqrt{36}} = \frac{1}{6}$$

*Just a reminder.
Exponent Rules

$$a^0 = 1 \quad \text{if } a \neq 0$$

$$a^{-n} = \frac{1}{a^n} \quad \text{or} \quad \frac{1}{a^{-n}} = a^n \quad \text{if } a \neq 0$$

$$a^m \cdot a^n = a^{m+n}$$

$$\frac{a^m}{a^n} = a^{m-n} \quad \text{if } a \neq 0$$

$$(a^m)^n = a^{m \cdot n}$$

$$(a \cdot b)^n = a^n \cdot b^n$$

$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n} \quad \text{if } b \neq 0$$

$$\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n \quad \text{if } a \neq 0, b \neq 0$$

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(F) After you simplify you should have:

- Only positive exponents.
- Each base only occurring once.
- Have no parentheses in the expression.
- No powers written to powers.

Simplify using properties of exponents. Leave answers with rational exponents

$$\frac{1}{2} + \frac{1}{3} \stackrel{\text{use calc}}{\text{or}} \frac{3x}{6} + \frac{x}{6} = \frac{5}{6}$$

$$x^{\frac{1}{2}} \cdot x^{\frac{1}{3}} = x^{\frac{5}{6}}$$

$$\frac{\frac{1}{3} - \frac{5}{3}}{-\frac{4}{3}} \cdot \frac{x^{\frac{1}{3}}}{x^{\frac{5}{3}}} = x^{-\frac{4}{3}} = \frac{1}{x^{\frac{4}{3}}}$$

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You Try

$$r^{\frac{3}{4}} \cdot r^{\frac{1}{6}}$$

$$\frac{x^{\frac{2}{3}}}{x^{\frac{1}{5}}}$$

Simplify each of the following:

$$\left(x^{\frac{2}{5}} \right)^{\frac{5}{4}} = x^{\frac{1}{2}}$$

$$\frac{\frac{1}{2} \cdot \frac{3}{2} = \frac{3}{4}}{\frac{2}{3} \cdot \frac{3}{2} = 1} \left(x^{\frac{1}{2}} \cdot y^{\frac{2}{3}} \right)^{\frac{3}{2}} = x^{\frac{3}{4}} y$$

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You Try

$$\left(100^{\frac{3}{8}} \right)^{\frac{4}{3}}$$

$$\left(a^{\frac{3}{2}} \cdot b^{\frac{5}{4}} \right)^{\frac{2}{3}}$$

Simplify the following:

$$\left(16x^{-4}y^6 \right)^{-\frac{3}{2}} = 16^{-\frac{3}{2}} x^6 y^{-9} = \frac{x^6}{16^{\frac{3}{2}} y^9}$$

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Use rational exponents to simplify the radicals.

$$\frac{\sqrt{x}}{\sqrt[3]{x^2}}$$

$$\sqrt[3]{z}$$

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Attachments

1-4 Rational Exponents - Calculator task.docx